Special forms of quadratic functions reveal ordered pair locations of key parabola points.

| Standard Form $f(x)=a x^{2}+b x+c$ <br> y-intercept <br> ( $0, ~ c$ ) | Factored Form $\begin{gathered} f(x)=a(x-m)(x-n) \\ x \text {-intercepts } \\ (m, 0) \&(n, 0) \end{gathered}$ | Vertex Form $f(x)=a(x-h)^{2}+\mathbf{k}$ <br> Vertex <br> (h, k) |
| :---: | :---: | :---: |
| Note: Values in parentheses come out as opposites. |  |  |
| $f(x)=-2 x^{2}+4 x+6 \quad$ |  |  |
|  |  |  |
| y-intercept (0,6) |  |  |
| $f(x)=-2(x+1)(x-3)$ |  |  |
|  |  |  |
| $x$-intercepts $(-1,0) \&(3,0)$ |  |  |
| $f(x)=-2(x-1)^{2}+8$ |  | $(3,0)$ |
| Vertex (1,8) |  |  |
|  |  |  |

## CFU

Which quadratic function has a $y$-intercept at (0, -7 )? Explain.
(A) $f(x)=x^{2}-6 x-7$
(B) $f(x)=(x+6)^{2}-7$
(C) $f(x)=(x+6)(x-7)$

Which quadratic function has $\mathbf{x}$-intercepts at $(5,0)$ and $(-8,0)$ ? Explain.
(A) $f(x)=5(x-5)^{2}-8$
(B) $f(x)=5 x^{2}+5 x-8$
(C) $f(x)=5(x-5)(x+8)$

Which quadratic function has a vertex location (-4, 10)? Explain.
$\begin{aligned} \text { (A) } f(x) & =-3(x-4)^{2}+10 \\ \text { (B) } f(x) & =-2(x+4)(x-10) \\ \text { (C) } f(x) & =(x+4)^{2}+10\end{aligned}$

1 Identify the y-intercept from the standard form.
2 Identify the x-intercepts from the factored form.
3 Identify the vertex from the vertex form.
4 Plot the points and sketch the graph.

1. $f(x)=-2(x+1)(x+7)$

$$
f(x)=-2 x^{2}-16 x-14
$$

$$
f(x)=-2(x+4)^{2}+18
$$


maximum or minimum


1 Identify the y-intercept from the standard form.
2 Identify the x-intercepts from the factored form.
3 Identify the vertex from the vertex form.
4 Plot the points and sketch the graph.
2. $f(x)=(x-3)^{2}-4$

$$
f(x)=(x-5)(x-1)
$$

$$
f(x)=x^{2}-6 x+5
$$

| $y$-intercept | x | $f(x)$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum


## Skill Closure

1 Identify the y-intercept from the standard form.
2 Identify the x-intercepts from the factored form.
3 Identify the vertex from the vertex form.
4 Plot the points and sketch the graph.
1.

$$
\begin{aligned}
& f(x)=(x+2)(x-4) \\
& f(x)=x^{2}-2 x-8 \\
& f(x)=(x-1)^{2}-9
\end{aligned}
$$

| $y$-intercept | x | $\mathrm{f}(\mathrm{x})$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum


## Concept Closure

If there is an error in the table, identify and explain it. If not, select "No errors were made."

$$
\begin{aligned}
& f(x)=-3 x^{2}+18 x-15 \\
& f(x)=-3(x-1)(x-5) \\
& f(x)=-3(x-3)^{2}+12
\end{aligned}
$$

|  | $x$ | $f(x)$ |
| :---: | :---: | :---: |
| y-intercept | 0 | -15 |
| x-intercepts - | 1 | 0 |
|  | -5 | 0 |
|  | 3 | 12 |
|  |  |  |

No errors were made.

Standard Form $f(x)=a x^{2}+b x+c$ $y$-intercept ( $0, ~ c$ )

Factored Form $f(x)=a(x-m)(x-n)$
x-intercepts
$(m, 0) \&(n, 0)$
Vertex Form
$f(x)=a(x-h)^{2}+k$ Vertex
(h, k)

1 Identify the y-intercept from the standard form.
2 Identify the x-intercepts from the factored form.
3 Identify the vertex from the vertex form.
4 Plot the points and sketch the graph.

1. $f(x)=3(x+1)^{2}-12$

$$
f(x)=3(x+3)(x-1)
$$

$$
f(x)=3 x^{2}+6 x-9
$$

| y-intercept | x | $f(x)$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum
2. $f(x)=-(x-3)(x-5)$

$$
f(x)=-x^{2}+8 x-15
$$

$$
f(x)=-(x-4)^{2}+1
$$

| $y$-intercept | X | $f(x)$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  | maximum or minimum

Find key parabola points and graph them.
1.

$$
\begin{aligned}
& f(x)=-5(x+3)(x+1) \\
& f(x)=-5 x^{2}-20 x-15 \\
& f(x)=-5(x+2)^{2}+5
\end{aligned}
$$

| $y$-intercept | x | $\mathrm{f}(\mathrm{x})$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum
2.

$$
\begin{aligned}
& f(x)=4(x-2)^{2}-4 \\
& f(x)=4(x-1)(x-3) \\
& f(x)=4 x^{2}-16 x+12
\end{aligned}
$$

| y-intercept | X | $\mathrm{f}(\mathrm{x})$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum



If there is an error in the table, identify and explain it. If not, select "No errors were made."
3.

$$
\begin{aligned}
& f(x)=x^{2}+10 x+16 \\
& f(x)=(x+2)(x+8) \\
& f(x)=(x+5)^{2}-9
\end{aligned}
$$

| $y$-intercept | x | $f(x)$ |
| :---: | :---: | :---: |
|  | 0 | 16 |
|  | -2 | 0 |
| x-intercepis | -8 | 0 |
| vertex | 5 | 9 |

No errors were made.

Find key parabola points and graph them.
1.

$$
\begin{aligned}
& f(x)=-2(x-4)(x-2) \\
& f(x)=-2 x^{2}+12 x-16 \\
& f(x)=-2(x-3)^{2}+2
\end{aligned}
$$

| y-intercept | x | $f(x)$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum
2.

$$
\begin{aligned}
& f(x)=-(x+8)(x+2) \\
& f(x)=-x^{2}-10 x-16 \\
& f(x)=-(x+5)^{2}+9
\end{aligned}
$$

| y-intercept | X | $\mathrm{f}(\mathrm{x})$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum



If there is an error in the table, identify and explain it. If not, select "No errors were made."
3.

$$
\begin{aligned}
& f(x)=-2 x^{2}-8 x+42 \\
& f(x)=-2(x-3)(x+7) \\
& f(x)=-2(x+2)^{2}+50
\end{aligned}
$$

|  | $x$ | $f(x)$ |
| :---: | :---: | :---: |
|  | $y$-intercept | 0 |
| x-intercepts | -2 |  |
|  | -2 | 0 |
|  | -8 | 0 |
|  | 5 | 9 |
|  |  |  |

No errors were made.

Find key parabola points and graph them.
1.

$$
\begin{aligned}
& f(x)=(x-5)^{2}-16 \\
& f(x)=(x-1)(x-9) \\
& f(x)=x^{2}-10 x+9
\end{aligned}
$$


maximum or minimum
2.

$$
\begin{aligned}
& f(x)=2(x+3)^{2}-18 \\
& f(x)=2(x+6)(x+0) \\
& f(x)=2 x^{2}+12 x
\end{aligned}
$$

| $y$-intercept | X | $f(x)$ |
| :---: | :---: | :---: |
|  |  |  |
| x-intercepts |  |  |
|  |  |  |
| vertex |  |  |

maximum or minimum



If there is an error in the table, identify and explain it. If not, select "No errors were made."
3.

$$
\begin{aligned}
& f(x)=x^{2}-12 x+27 \\
& f(x)=(x-3)(x-9) \\
& f(x)=(x-6)^{2}-9
\end{aligned}
$$

| y-intercept | X | f(x) |
| :---: | :---: | :---: |
|  | 0 | 16 |
| x-intercepts | -2 | 0 |
|  | -8 | 0 |
| vertex | 5 | 9 |

